

## Regular article

# Theoretical spectroscopic constants of the GaN molecule

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Received: 14 July 1998 / Accepted: 17 September 1998 / Published online: 7 December 1998

**Abstract.** Fourth-order multi-reference coupled pair approximation (MRCPA-4) calculations were performed to predict spectroscopic constants of the gallium nitride (GaN) diatomic molecule. The calculations showed that the ground state is  $^3\Sigma^-$  but that the  $^3\Pi$  state is low lying and separated from the former by 0.5 eV. The contribution of the correlations among the Ga 3*d* semi-core electrons was found to be crucial for a quantitative description of the molecule.

**Key words:** Gallium nitride – Semi-core electrons – Near degeneracy – Size consistency – Multi-reference coupled pair approximation

## 1 Introduction

In our previous studies [1, 2], spectroscopic constants of the gallium hydride (GaH) and gallium fluoride (GaF) molecules, and their positive ions, were calculated by the fourth-order coupled pair approximation (CPA-4) and its MR variant (MRCPA-4) [3–7] with flexible basis sets. It was shown that the electron correlations of the Ga 3*d* semi-core shell have a sizable contribution in evaluating spectroscopic constants, with a quantitative agreement with experiment. Inclusion of not only the valence/3*d* intershell but also the 3*d* intrashell correlations was found to be necessary for the balanced and thus reliable description, although it was computationally costly. The formation of chemical bonds by the valence 4*s* and 4*p* electrons on Ga could induce differential effects on the 3*d* electrons relative to the purely atomic environment.

In a series of investigations, we predict spectroscopic constants of the gallium nitride (GaN) molecule, using the similar scheme of calculations as with our previous papers [1, 2]. No experimental or theoretical information, including the assignment of the ground state, was available for this molecule to date, although its existence has been predicted. GaN solids, which are semi-conductors, are well known to be promising emitter material for blue-region light (e.g. see [8]). Thus, experimental investigation for the growth processes, stable surface phases, and electronic properties have been extensively carried out for the solid state. Correspondingly, density-functional theory (DFT) calculations have been reported. Some of such DFT calculations took special care in treating the Ga 3*d* shell, using the so-called non-linear core correction (NLCC) in conjunction with the pseudo-potential technique [9–11]. The NLCC could incorporate the exchange and correlation contributions from the 3*d* electrons in an effective fashion. If the NLCC is not considered, the reliability of the numerical evaluation is not acceptable for a quantitative discussion of GaN solids [11]. From the viewpoint of the orbital energy, the levels of Ga 3*d* and N 2*s* are close to each other, where the values are  $-1.15$  au for the former and  $-0.93$  au for the latter according to the atomic self-consistent-field (SCF) procedure [12]. When the bonds form between Ga and N atoms, interactions between the N 2*s* and Ga 3*d* orbitals cannot be negligible because of such an energetic closeness. A balanced treatment for 3*d* and 2*s* would be required for a quantitative description of the Ga-N bonding.

Now, the fundamental issue to be solved is the determination of the ground state of the diatomic GaN molecule. By analogy with the isovalent molecules BN, AlN, AlP, and GaAs [13–21], there are two possible candidates:  $^3\Sigma^-$  and  $^3\Pi$ . The former state has a single  $\sigma$  bond and the latter has a  $\pi$  bond. The energetic separation between the  $^3\Sigma^-$  and  $^3\Pi$  states of these species is known to be small. For example, Langhoff et al. [19] calculated that the ground state of AlN is  $^3\Pi$ , using the complete-active-space self-consistent-field (CASSCF) [22] and multi-reference configuration interaction (MRCI)

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methods. Their assignment has been in accord with experimental observation and later calculations [20, 21]. Langhoff et al. showed that the adiabatic excitation energy ( $T_e$ ) for the  $^3\Sigma^-$  first excited state of AlN is less than 0.1 eV, where its energetic separation depends on the level of theory. The ground state of GaAs has been settled as  $^3\Sigma^-$ . The calculated separation from  $^3\Pi$  was as small as  $\sim 0.2$  eV for GaAs by MRCI investigations [14–17]. For both AlN and GaAs molecules, a much shorter bond length ( $R_e$ ) for  $^3\Pi$  was evaluated than for that of  $^3\Sigma^-$ . The situation in GaN may be the same. Furthermore, the introduction of Ga  $3d$  correlations can provide for the contraction of  $R_e$ , as was demonstrated for the neutral state of GaH and GaF [1, 2]. Thus, for the GaN molecule, we would have a special interest in the relation between the  $^3\Sigma^-$ - $^3\Pi$  separation and the  $R_e$  value.

The remainder of the present paper is configured as follows. In Sect. 2, a qualitative bonding picture is given for the  $^3\Sigma^-$  and  $^3\Pi$  states, based on the results of preliminary calculations. Near degeneracies exist among the bonding and anti-bonding orbitals, and this requires MRCPA-4 treatment for both states. Details of the MRCPA-4 calculations are described in Sect. 3. Section 4 presents the spectroscopic constants for each state.

## 2 Qualitative bonding picture

The atomic ground state of the Ga atom is  $^2P$  by the valence configuration of  $4s^2 4p^1$  on the  $3d$  semi-core shell. The N atom has the  $^4S$  ground state by the  $2s^2 2p^3$  configuration, where  $2s$  is referred to as a valence shell. The following discussions are derived from preliminary calculations; the basis sets used for Ga and N are the same as the main calculations (refer to the first paragraph in Sect. 3).

When Ga and N atoms make a  $\sigma$  bond with  $p$ -type atomic orbitals (AOs), this leads to the  $^3\Sigma^-$  state. Preliminary calculations indicated that this state seems to be the ground state. The main (or an SCF-type) configuration of  $^3\Sigma^-$  is symbolically described as  $\sigma_b^2 \pi_{b(x)}^1 \pi_{b(y)}^1$ . The subscript “b” for these molecular orbitals (MOs) means the “bonding” (or in-phase) combination between Ga  $4p$  and N  $2p$  AOs. Owing to the electronegativity of N, the component of the  $\sigma_b$  MO is characterized as  $\lambda 4p + 2p$ , where  $\lambda$  is a small mixing parameter. Two electrons in  $\pi_{b(x,y)}$  orbitals are attributed essentially to N  $2p$  electrons but contribute to the total stabilization since delocalization toward the Ga  $4p$  side takes place. These contributions in the  $^3\Sigma^-$  state may be considered as two additional “one-electron bonds” of the  $\pi$  type.

The  $^3\Pi$  state has a regular “two-electron bond” of the  $\pi$  type, where the orbital is denoted again as  $\pi_b$  and has a similar component character to  $\sigma_b$ . In the  $C_{2v}$  subset of the full  $C_{\infty v}$  symmetry, the main configuration may be written as  $\sigma_b^1 \pi_{b(x)}^2 \pi_{b(y)}^1$ . The state has additionally two “one-electron bonds” of  $\sigma$  and  $\pi$  types. For the isovalent AlN molecule, Langhoff et al. [19] pointed out that multi-reference character is prominent, especially in the  $^3\Pi$  state. The present GaN molecule has similar features to AlN. By CASSCF calculations of a  $4s 4p/2p$  (six

electrons in seven orbitals) type, the  $\pi_{b(x)}^2 \rightarrow \pi_{ab(x)}^2$  excitation among bonding and anti-bonding MOs is observed to be responsible for the principal part of the near degeneracies in the  $^3\Pi$  state, where the latter MO has the counter-mixing character of  $4p-\lambda' 2p$ . The occupation numbers of active space natural orbitals (NOs) are calculated to be 1.8 for  $\pi_{b(x)}$  and 0.2 for  $\pi_{ab(x)}$ , even around  $R_e$ , for the  $^3\Pi$  state. In contrast, values for the  $^3\Sigma^-$  state are roughly 1.97 for  $\sigma_b$  and 0.03 for  $\sigma_{ab}$ . The near degeneracy of  $\sigma_b^2 \rightarrow \sigma_{ab}^2$  certainly exists in  $^3\Sigma^-$ , but its degree is less than  $^3\Pi$ , although a proper MR treatment is needed for both states. Through these CASSCF calculations, the much shorter  $R_e$  is obtained for the  $^3\Pi$  state.

## 3 Details of MR calculations

The Gaussian basis set used for the Ga atom was the same as in the previous calculations [1, 2]. Thus, the Ga contracted set was  $(15s12p7d4f2g)/[9s7p5d3f1g]$ , where the fundamental part of this set is due to Schäfer et al. [23]. Preparation of augmentation functions was described in [1]. The N basis set was  $[7s4p3d2f]$ , derived similarly from then F case [2]. The basic  $[6s3p]$  part was due to Schäfer et al. [23], the polarization and/or correlating functions of  $[3d2f]$  were taken from “aug-cc-pVTZ” by Dunning et al. [24, 25]. Exponents of the augmented diffuse  $s$  and  $p$  functions were 0.0598 and 0.0477, respectively. Basis set data, except for the authors’ augmentation, were obtained from the internet database server at the US Pacific Northwest National Laboratory [26]. Cartesian contaminants of  $d$ ,  $f$ , and  $g$  functions were deleted, and the total number of basis functions was 133.

The CASSCF procedure, in which a rather minimal active space was defined according to the results of preliminary calculations, was used to prepare the input MO set for MRCPA-4. The CAS problem was that six electrons are distributed among five orbitals for both the  $^3\Sigma^-$  and  $^3\Pi$  states. The  $C_{2v}$  symmetry instead of  $C_{\infty v}$  was actually used, as was addressed in Sect. 2. The active orbital space for  $^3\Sigma^-$ , which was represented as  $^3A_2$  in  $C_{2v}$ , was composed of three  $a_1$ , one  $b_1$ , and one  $b_2$  orbitals. Three  $a_1$  active MOs consisted essentially of Ga  $4s$ ,  $4p\sigma$ , and N  $2p\sigma$  AOs, and thus the near degeneracy between  $\sigma_b$  and  $\sigma_{ab}$  could be described with a flexibility of hybridization between Ga  $4s$  and  $4p$ . The  $4s$ -dominated MO is denoted as  $\sigma_{4s}$ . The  $b_1$  and  $b_2$  active MOs corresponded to  $\pi_{b(x,y)}$  dominated by N  $2p\pi$ . For the  $^3\Pi$  or  $^3B_2$  state, the  $4p\sigma$  ( $a_1$ ) orbital of  $^3\Sigma^-$  was replaced by  $4p\pi_{(x)}$  ( $b_1$ ) for description of the crucial  $\pi_{b(x)}^2 \rightarrow \pi_{ab(x)}^2$  double excitation. The total numbers of configurations in CAS-CI for  $^3\Sigma^-$  and  $^3\Pi$  were six and eight, respectively. The numbers in configuration state functions (CSFs) were 12 for both states.

The mixing between Ga  $3d\sigma$  and N  $2s$  orbitals was actually found, especially for the  $^3\Pi$  state having the closer Ga-N distance than  $^3\Sigma^-$ . The orbital energy of a “ $3d\sigma$ ” type MO is lowered and that of a “ $2s$ ” is raised by the mixing. In previous studies for GaH [1] and GaF [2], the following correlating schemes were used:

1.  $V$ : only valence electrons are correlated.
2.  $CV$ : semi-core electrons are additionally correlated, but simultaneous two-electron excitations are not involved from the semi-core shells.
3.  $C$ : valence and semi-core electrons are correlated at the same footing.

However, an imbalance in the  $CV$  scheme, in which the intra  $3d$  shell correlation is not taken into account but the N  $2s$  shell is normally correlated as valence, was suspected because of the orbital interaction denoted above. To check this suspicion, a set of SCF-reference CPA-4 calculations by the  $V$ ,  $CV$ , and  $C$  schemes was

carried out for the  ${}^3\Sigma^-$  state, which has less near-degeneracy than does the  ${}^3\Pi$  state. The resulting  $R_e$  values for  $V$ ,  $CV$ , and  $C$  schemes are 3.91 au, 3.68 au, and 3.83 au, respectively. The bond contraction by the  $CV$  scheme looks overestimated, and consequently the  $V$  and  $C$  schemes were employed for the MRCPA-4 calculations.

In generating singly and doubly excited CSFs, the SCF-type configuration (being the single CSF) and the bonding/anti-bonding doubly excited configuration (also the single CSF) in the CASSCF wavefunction were used as the reference set:

$${}^3\Sigma^- ({}^3A_2) : (1)\sigma_{4s}^2\sigma_b^2\pi_{b(x)}^1\pi_{b(y)}^1, (2)\sigma_b^2 \rightarrow \sigma_{ab}^2$$

$${}^3\Pi ({}^3B_2) : (1)\sigma_{4s}^2\sigma_b^1\pi_{b(x)}^1\pi_{b(y)}^1, (2)\pi_{b(x)}^2 \rightarrow \pi_{ab(x)}^2$$

All possible spin-couplings for each excited configuration were taken in the CSF generation. The highest five ( $3 \times a_1, b_1,$  and  $b_2$ ) external MOs were kept unoccupied since these MOs have the radial node in the core region [2]. The lengths of the expansions for the  $C$  scheme, in which total of 18 electrons were correlated, were 971 570 for  ${}^3\Sigma^-$  and 964 435 for  ${}^3\Pi$ . For the  ${}^3\Sigma^-$  state, three CSFs associated with the singly excited configuration of  $\sigma_b \rightarrow \sigma_{ab}$  were included as the zeroth-order space to be pre-diagonalized since these CSFs were potentially of an ‘‘intruder’’ type [3–7], although the contribution at the CASSCF stage was small. Thus, the notation of 2R(+1)CPA-4 is used for  ${}^3\Sigma^-$  henceforth. The number of CSFs for 2R(+1) was five. In contrast, all the CSFs of remaining six configurations in CAS-CI were treated in the zeroth-order space for  ${}^3\Pi$ , and thus its notation was 2R(+6)CPA-4 (or the dimension of zeroth-order space was 12, the same as the CAS-CI). 2RCI calculations were carried out in parallel for a cross-check purpose. For the  ${}^3\Pi$  state, 3RCI calculations, in which the  $\pi_b \rightarrow \pi_{ab}$  singly excited configuration was additionally used for the reference configurations, were also performed, where its expansion length was 2 297 441. Davidson’s correction, denoted as + $Q$  [27], was added to CI energies for a remediation of the lack of size consistency.

Values of the bond energy ( $D_e$ ) for  ${}^3\Sigma^-$  were evaluated in two ways, as was done previously [2]. The first way was the so-called supermolecule (SM) approach, where the state of the dissociation limit was set to the high-spin  ${}^5\Sigma^-$  with a Ga-N distance of 100 au. The second way was due to the sum of separated atom energies (SAE). At the  $C$  level of calculation, the expansion length for SM was as large as 3 098 797 and we were unfortunately unable to perform the CPA-4 calculation. Thus, only the SAE value was available for the C-2R(+1)CPA-4 case, but the difference of that from SM was expected to be small since (MR)CPA-4 has a size consistency [2–7]. A multiplicity-averaged spin-orbit splitting of  $-0.07$  eV for the Ga ( ${}^2P_{1/2}-{}^2P_{3/2}$ ) atom [28] was corrected for  $D_e$  [1, 2]. The atomic masses for Ga and N in the vibrational frequency ( $\omega_e$ ) evaluation were 68.9256 and 14.0067, respectively.

#### 4 Spectroscopic constants of ${}^3\Sigma^-$ and ${}^3\Pi$

Table 1 summarizes the spectroscopic constants  $D_e$ ,  $R_e$ , and  $\omega_e$  for the  ${}^3\Sigma^-$  ground state. In this table, results due to the zeroth-order space of 2R(+1) in CPA-4 are also included.  $D_e$  results are first focused on. One can see immediately that the difference between the SM and SAE (in parentheses) approaches is reasonably small for CPA-4, but the difference is unacceptable for CI even with Davidson’s correction at the  $C$  level of treatment. This is a quite similar situation to the previous case of GaF [2]. Size consistency is an essential requirement.

Through the introduction of correlations,  $D_e$  is increased from the 1.11 eV which has been calculated by the zeroth-order treatment of 2R(+1). This illustrates the importance of the differential correlation energy for the estimation of bond formation. Even by the  $V$  scheme, the increment is as large as  $\sim 0.7$  eV. Introduction of the  $3d$  electron correlation through C-2R(+1)

**Table 1.** Spectroscopic constants for gallium nitride (GaN) in the  ${}^3\Sigma^-$  ground state

Method	$D_e$ (eV) <sup>a,b,c</sup>	$R_e$ (au)	$\omega_e$ (cm <sup>-1</sup> )
2R(+1)	1.11	3.83	477
$V$			
2RCI	1.76 (1.56)	3.81	506
2RCI + Q	1.85 (1.80)	3.83	494
2R(+1)CPA-4	1.86 (1.88)	3.82	505
$C$			
2RCI	1.76 (1.22)	3.76	523
2RCI + Q	1.90 (1.69)	3.77	515
2R(+1)CPA-4	(1.95)	3.76	546

<sup>a</sup>A multiplicity-averaged spin-orbit splitting for the Ga atom ( $-0.07$  eV [28]) was taken into account for the present calculations, as in [1, 2]

<sup>b</sup>Calculated  $D_e$  in parentheses was due to the ‘‘sum of atomic energies’’ scheme. Refer to text

<sup>c</sup>Total energies are  $-1977.6087$  au for 2R(+1),  $-1977.8107$  au for  $V$ -2R(+1)CPA-4, and  $-1978.2413$  au for C-2R(+1)CPA-4 (at each  $R_e$ ). Thus, the correlation energies for the  $V$  and  $C$  schemes of CPA-4 are 5.50 eV and 17.21 eV, respectively. CI energies are omitted here because of a lack of size consistency

CPA-4 adds 0.07 eV according to the SAE approach and provides the value 1.95 eV as the best  $D_e$  prediction for the GaN molecule. Balasubramanian [15] reported 1.9 eV for the isovalent GaAs molecule by the CASSCF procedure followed by second-order MRCI (so-called SOCI), where he used a couple of special corrections including Meier’s value of 0.2 eV [16] for the  $3d$  correlations of both Ga and As atoms. For AlN, the  $D_e$  value was calculated to be 2.3 eV [16] by the MRCI+Q level for the  ${}^3\Sigma^-$  state [19]. The predicted  $D_e$  of GaN would be comparable to those of GaAs and AlN.

$R_e$  and  $\omega_e$  values present an impact of correlation contribution of semi-core  $3d$  electrons. By the C-2R(+1)CPA-4 calculation,  $R_e$  is contracted by  $-0.06$  au and  $\omega_e$  is increased by  $41$  cm<sup>-1</sup>. As the best results, 3.76 au for  $R_e$  and 546 cm<sup>-1</sup> for  $\omega_e$  are predicted. The C-2RCI+Q procedure provides a preferable contraction for  $R_e$  but does not work for  $\omega_e$ . An inherently size-consistent method is highly required for such as the present type of theoretical investigations.

At the  $R_e$  by C-2R(+1)CPA-4, the dipole moment is calculated to be 1.69 D with the direction of Ga <sup>$\delta^+$</sup> -N <sup>$\delta^-$</sup> . The  $\sigma_b$  orbital is being characterized as  $\lambda 4p + 2p$  but this polarity of charge is somewhat compensated by delocalizations of two N  $2p\pi$  electrons toward the Ga  $4p\pi$  side in  $\pi_b$  MOs. A similar charge compensation to this was found in the GaF case [2].

The occupation numbers of C-2R(+1) CPA-4 resulting NOs are 1.89 for the  $\sigma_b$  type and 0.06 for  $\sigma_{ab}$ , where the weight of the zeroth-order space is 84%. The necessity of the MR scheme for GaN is well demonstrated here. This situation in GaN is quite different from the GaH and GaF cases, in which no tangible near-degeneracy was observed for the  $\sigma$  bonding [1, 2].

Now, the  $\pi$ -bonding  ${}^3\Pi$  state is discussed. Table 2 summarizes spectroscopic constants for this state. Instead of  $D_e$  in Table 1 for  ${}^3\Sigma^-$ ,  $T_e$  values are shown in this table. One can observe a relation between  $T_e$  and  $R_e$ , depending on the treatment of the correlation. The

**Table 2.** Spectroscopic constants for GaN in the  $^3\Pi$  first excited state

Method	$T_e$ (eV)	$R_e$ (au)	$\omega_e$ ( $\text{cm}^{-1}$ )
<i>V</i>			
2RCI	0.27	3.61	591
2RCI + Q	0.12	3.62	584
3RCI	0.14	3.60	600
3RCI + Q	-0.03	3.61	597
2R(+6)CPA-4	0.29	3.64	583
<i>C</i>			
2RCI	0.34	3.53	607
2RCI + Q	0.20	3.51	605
3RCI	0.20	3.49	618
3RCI + Q	0.09	3.49	616
2R(+6)CPA-4	0.50	3.57	637

*C*-2R(+6)CPA-4 calculation provides 0.5 eV as the best  $T_e$  prediction at its  $R_e$  of 3.57 au. By the *V* scheme, the separation is only 0.29 eV at  $R_e$  of 3.64 au. The introduction of semi-core  $3d$  correlation leads to the contraction of  $-0.07$  au for  $R_e$  and the increase of  $54 \text{ cm}^{-1}$ . The amount of these numerical shifts provided by the *C* scheme is similar to the  $^3\Sigma^-$  state (refer to Table 1). CI results are again found to be inferior to CPA-4, even at the 3R level of reference setting.  $T_e$  estimates with +Q correction seem to be too small or overshoot.

The occupation numbers of NOs by *C*-2R(+6)CPA-4 are 1.88 for  $\pi_b$  and 0.1 for  $\pi_{ab}$  at  $R_e$ , where the weight of the zeroth-order space is 83%. The larger occupation in  $\pi_{ab}$  than  $\sigma_{ab}$  for the  $^3\Sigma^-$  state (recall the value of 0.06) clearly illustrates that there is the more severe near-degeneracy in the  $\pi$  bond. The dipole moment is calculated to be 1.61 D for the  $^3\Pi$  state.

According to the *C* scheme CPA-4 calculations, the  $^3\Pi$  states has the shorter  $R_e$  by  $-0.19$  au and the larger  $\omega_e$  by  $+91 \text{ cm}^{-1}$  than those of the  $^3\Sigma^-$  state. The shorter  $R_e$  for  $^3\Pi$  reflects the fact that the  $\pi$  bonding requires the closer Ga-N distance for the better overlap between  $4p\pi$  and  $2p\pi$  AOs owing to a symmetrical reason. The higher  $\omega_e$  for  $^3\Pi$  is in accord with this nature. Higher frequencies for the  $\pi$  bonding state than  $\sigma$  bonding case have been found previously [13–16, 19]. The transition of  $^3\Sigma^- \rightarrow ^3\Pi$  is of a dipole-allowed type in the infrared region. However, the (0, 0) vibrational transition is expected to be weak because of a sizable difference in  $R_e$ , as was pointed out by Meier et al. [16] for the GaAs molecule based on the evaluation of Franck-Condon factors. Such an analysis, which should require a wide range of potential energy curves and the vibrational wavefunctions for GaN, may be a future subject.

## 5 Summary

Spectroscopic constants of the GaN diatomic molecule were predicted, based on MRCPA-4 calculations in which both the near-degeneracy in valence bonding and the correlation among Ga  $3d$  semi-core electrons were taken into account. The ground state was revealed to be the  $\sigma$ -bonding  $^3\Sigma^-$  state. Its  $D_e$  value was evaluated to be 1.95 eV.  $R_e$  and  $\omega_e$  were 3.76 au and  $546 \text{ cm}^{-1}$ , respec-

tively. The  $\pi$ -bonding  $^3\Pi$  state was shown to be low lying with a  $T_e$  of 0.5 eV. A considerably shorter  $R_e$  of 3.57 au was obtained for  $^3\Pi$ , indicating the need for a closer distance for  $\pi$  bonding.

*Acknowledgements.* Work reported in this paper was partly done under a contract for collaborative investigations between the Fundamental Research Laboratories of the NEC Corporation (to which Y.M. belonged until the fall of 1997) and K.T.'s laboratory at The University of Electro-Communications (UEC). K.T. moved to Hokkaido University in the Spring of 1998, and the calculations and analyses have recently been completed there. Y.M. thanks the NEC and UEC for support for part of the present investigations. Support by the Japan Science and Technology Corporation (JST) and the Japan Atomic Energy Research Institute (JAERI) are also appreciated by Y.M.; both of these organizations are operated by the Science and Technology Agency (STA) of the Japanese government. All the calculations were carried out using the codes of Alchemy-II [29–32] and direct-CPA [5, 6] on IBM RS-6000 workstations managed by K.T.

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- part of the Pacific Northwest National laboratory, PO Box 999, Richland, Washington 99352, USA, and funded by the U.S. Department of Energy. The Pacific Northwest National Laboratory is a multi-program laboratory operated by Battelle Memorial Institute for the U.S. Department of Energy under contract DE-AC06-76RLO 1830. Please contact Drs. D. Feller, K. Schuchardt, or D. Jones for further information
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